

First I name the matrix of our system.

```
In[1]:= mA = {{3, 0, -1, 1}, {1, 1, -2, 2}, {2, -1, 1, 3}}
```

```
Out[1]= {{3, 0, -1, 1}, {1, 1, -2, 2}, {2, -1, 1, 3}}
```

To display this matrix in the traditional form I use

```
In[2]:= MatrixForm[mA]
```

```
Out[2]//MatrixForm=
```

$$\begin{pmatrix} 3 & 0 & -1 & 1 \\ 1 & 1 & -2 & 2 \\ 2 & -1 & 1 & 3 \end{pmatrix}$$

Now I row reduce the matrix mA. The command that performs row reduction is applied to the matrix mA and then, MatrixForm displays the result in convenient form:

```
In[3]:= MatrixForm[RowReduce[mA]]
```

```
Out[3]//MatrixForm=
```

$$\begin{pmatrix} 1 & 0 & -\frac{1}{3} & 0 \\ 0 & 1 & -\frac{5}{3} & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

What I see is that each row has a pivot entry. This tells me that whatever the augmented column is, the system with this matrix will always have a solution. The reason for this is that a system with three equations can have at most three pivots. Here, all pivots are in the columns which belong to the system, so the augmented column cannot be a pivot column.

Now form the augmented matrix

```
In[6]:= mAa = {{3, 0, -1, 1, -2}, {1, 1, -2, 2, 3}, {2, -1, 1, 3, 8}}
```

```
Out[6]= {{3, 0, -1, 1, -2}, {1, 1, -2, 2, 3}, {2, -1, 1, 3, 8}}
```

```
In[7]:= MatrixForm[mAa]
```

```
Out[7]//MatrixForm=
```

$$\begin{pmatrix} 3 & 0 & -1 & 1 & -2 \\ 1 & 1 & -2 & 2 & 3 \\ 2 & -1 & 1 & 3 & 8 \end{pmatrix}$$

```
In[8]:= MatrixForm[RowReduce[mAa]]
```

```
Out[8]//MatrixForm=
```

$$\begin{pmatrix} 1 & 0 & -\frac{1}{3} & 0 & -\frac{7}{4} \\ 0 & 1 & -\frac{5}{3} & 0 & -\frac{7}{4} \\ 0 & 0 & 0 & 1 & \frac{13}{4} \end{pmatrix}$$