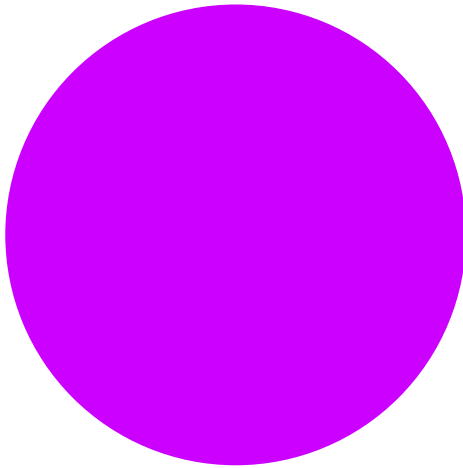


Here I demonstrate how to represent functions using colors.

Mathematica has many ways of communicating colors. The simplest one is `Hue[]`. The variable in `Hue` is between 0 and 1

```
In[63]:= Graphics[{Hue[0.8], Disk[{0, 0}, 1]}, PlotRange -> {{-1.5, 1.5}, {-1.5, 1.5}}]
```

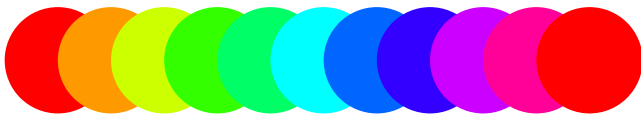
Out[63]=



Coloring 10 disks in different colors using `Hue[]`

```
In[64]:= Graphics[Table[{Hue[k/10], Disk[{k, 0}, 1]}, {k, 0, 10}],  
PlotRange -> {{-1.5, 11.5}, {-1.5, 1.5}}]
```

Out[64]=



Coloring 100 disks in different colors using `Hue[]`

```
In[65]:= Graphics[Table[{Hue[k/100], Disk[{k, 0}, 1]}, {k, 0, 100}],  
PlotRange -> {{-1.5, 101.5}, {-1.5, 1.5}}, ImageSize -> 400, AspectRatio -> 0.1]
```

Out[65]=



A convenient way of generating lists of numbers in *Mathematica* is offered by function `Range`

In[66]:= **Range[0, 1, 1 / 10]**

Out[66]= $\left\{0, \frac{1}{10}, \frac{2}{10}, \frac{3}{10}, \frac{4}{10}, \frac{5}{10}, \frac{6}{10}, \frac{7}{10}, \frac{8}{10}, \frac{9}{10}, 1\right\}$

A convenient way of applying a function to a list is given by so called pure function. To make the Sin function into a pure function we write

In[67]:= **Sin[#] &**

Out[67]= **Sin[#1] &**

But, more importantly, here is how to make the square function into a pure function

In[68]:= **(#^2) &[2]**

Out[68]= **4**

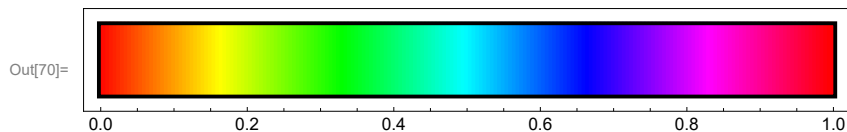
Apply the square to a list

In[69]:= **(#^2) & /@ Range[0, 1, 1 / 10]**

Out[69]= $\left\{0, \frac{1}{100}, \frac{4}{100}, \frac{9}{100}, \frac{16}{100}, \frac{25}{100}, \frac{36}{100}, \frac{49}{100}, \frac{64}{100}, \frac{81}{100}, 1\right\}$

Demonstrating Hue[] on the unit interval using many rectangles.

In[70]:= **st = $\frac{1}{200}$; cc = 0.002; hh = 0.1; LL = 1; Graphics[{ { Hue[#], Polygon[{ { # - $\frac{st}{2}$ - cc, 0}, { # + $\frac{st}{2}$ + cc, 0}, { # + $\frac{st}{2}$ + cc, hh}, { # - $\frac{st}{2}$ - cc, hh}, { # - $\frac{st}{2}$ - cc, 0} }] } & /@ Range[0 + $\frac{st}{2}$, LL - $\frac{st}{2}$, st], { Thickness[0.005], Line[{ { 0 - $\frac{st}{2}$, 0}, { LL + $\frac{st}{2}$, 0}, { LL + $\frac{st}{2}$, 0.1}, { 0 - $\frac{st}{2}$, 0.1}, { 0 - $\frac{st}{2}$, 0 } }] }] }, Frame -> True, FrameTicks -> { { None, None }, { Automatic, None } }, ImageSize -> 400]**

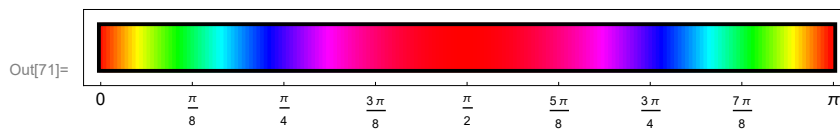


This is the sin function using Hue

```

In[71]:= st =  $\frac{\text{Pi}}{200}$ ; cc = 0.002; hh = 0.2; LL = Pi; Graphics[ {
  {Hue[Sin[#]], Polygon[{{# -  $\frac{\text{st}}{2}$  - cc, 0}, {# +  $\frac{\text{st}}{2}$  + cc, 0}, {# +  $\frac{\text{st}}{2}$  + cc, hh}, {# -  $\frac{\text{st}}{2}$  - cc, hh},
    {# -  $\frac{\text{st}}{2}$  - cc, 0}]}]} & /@ Range[0 +  $\frac{\text{st}}{2}$ , LL -  $\frac{\text{st}}{2}$ , st], {Thickness[0.005],
  Line[{{0 -  $\frac{\text{st}}{2}$ , 0}, {LL +  $\frac{\text{st}}{2}$ , 0}, {LL +  $\frac{\text{st}}{2}$ , hh}, {0 -  $\frac{\text{st}}{2}$ , hh}, {0 -  $\frac{\text{st}}{2}$ , 0}]}]}],
  Frame -> True, FrameTicks -> {{None, None}, {Range[0, Pi,  $\frac{\text{Pi}}{8}$ ], None}},
  ImageSize -> 400]

```



Next, I want to produce a coloring of the unit interval which will transition from white to red.

First, this is the Red Color

```
In[72]:= RGBColor[1, 0, 0]
```

Out[72]=

This is the White Color

```
In[73]:= RGBColor[1, 1, 1]
```

Out[73]=

How you transition from red to white is by using convex combination of vectors

```
In[74]:= (t) * {1, 0, 0} + (1 - t) {1, 1, 1}
```

Out[74]= {1, 1 - t, 1 - t}

At t = 0 we are at white

```
In[75]:= ((t) * {1, 0, 0} + (1 - t) {1, 1, 1}) /. {t -> 0}
```

Out[75]= {1, 1, 1}

At t = 1 we are red

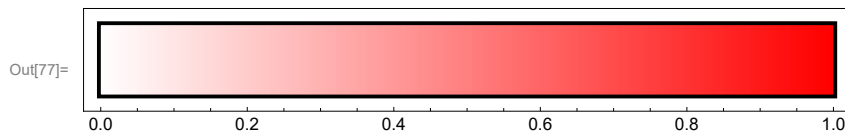
```
In[76]:= ((t) * {1, 0, 0} + (1 - t) {1, 1, 1}) /. {t -> 1}
```

Out[76]= {1, 0, 0}

```

In[77]:= st =  $\frac{1}{200}$ ; cc = 0.001; hh = 0.1; LL = 1; Graphics[ {
  {RGBColor[1, 1 - #, 1 - #], Polygon[ { {# -  $\frac{st}{2}$  - cc, 0},
    {# +  $\frac{st}{2}$  + cc, 0}, {# +  $\frac{st}{2}$  + cc, hh}, {# -  $\frac{st}{2}$  - cc, hh}, {# -  $\frac{st}{2}$  - cc, 0} } ] } & /@
  Range[0 +  $\frac{st}{2}$ , LL -  $\frac{st}{2}$ , st], {Thickness[0.005],
  Line[ { {0 -  $\frac{st}{2}$ , 0}, {LL +  $\frac{st}{2}$ , 0}, {LL +  $\frac{st}{2}$ , 0.1}, {0 -  $\frac{st}{2}$ , 0.1}, {0 -  $\frac{st}{2}$ , 0} } ] } ],
  Frame -> True, FrameTicks -> { {None, None}, {Automatic, None} },
  ImageSize -> 400 ]

```

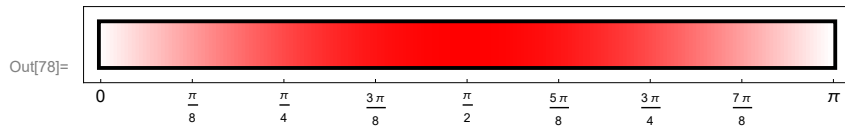


This is the sin function from 0 - white to 1 - red in the shades of red.

```

In[78]:= st =  $\frac{\pi}{200}$ ; cc = 0.002; hh = 0.2; LL = Pi; Graphics[ {
  {RGBColor[1, 1 - Sin[#], 1 - Sin[#]], Polygon[ { {# -  $\frac{st}{2}$  - cc, 0},
    {# +  $\frac{st}{2}$  + cc, 0}, {# +  $\frac{st}{2}$  + cc, hh}, {# -  $\frac{st}{2}$  - cc, hh}, {# -  $\frac{st}{2}$  - cc, 0} } ] } & /@
  Range[0 +  $\frac{st}{2}$ , LL -  $\frac{st}{2}$ , st], {Thickness[0.005],
  Line[ { {0 -  $\frac{st}{2}$ , 0}, {LL +  $\frac{st}{2}$ , 0}, {LL +  $\frac{st}{2}$ , hh}, {0 -  $\frac{st}{2}$ , hh}, {0 -  $\frac{st}{2}$ , 0} } ] } ],
  Frame -> True, FrameTicks -> { {None, None}, {Range[0, Pi,  $\frac{\pi}{8}$ ], None} },
  ImageSize -> 400 ]

```



These are the powers of Sin[x] function from 0 - white to 1 - red in the shades of red.

```

In[79]:= st =  $\frac{\text{Pi}}{200}$ ; cc = 0.002; hh = 0.2; LL = Pi;
Manipulate[Graphics[{
  {RGBColor[1, 1 - (Sin[#])nn, 1 - (Sin[#])nn],
  Polygon[{{# -  $\frac{\text{st}}$  - cc, 0}, {# +  $\frac{\text{st}}$  + cc, 0}, {# +  $\frac{\text{st}}$  + cc, hh}, {# -  $\frac{\text{st}}$  - cc, hh},
    {# -  $\frac{\text{st}}$  - cc, 0}]}] & /@ Range[0 +  $\frac{\text{st}}$ , LL -  $\frac{\text{st}}$ , st], {Thickness[0.005],
  Line[{{0 -  $\frac{\text{st}}$ , 0}, {LL +  $\frac{\text{st}}$ , 0}, {LL +  $\frac{\text{st}}$ , hh}, {0 -  $\frac{\text{st}}$ , hh}, {0 -  $\frac{\text{st}}$ , 0}]}]}],
  Frame → True, FrameTicks → {{None, None}, {Range[0, Pi,  $\frac{\text{Pi}}{8}$ ], None}},
  ImageSize → 400],
{nn, Range[1, 20], Setter, ControlPlacement → Top}]

```

Out[80]=

